ПATIBIA UחIVERSITY
OF SCIERCE ACD TECHOOLOGY
FACULTY OF COMPUTING AND INFORMATICS
DEPARTMENT OF COMPUTER SCIENCE

| QUALIFICATION: BACHELOR OF COMPUTER SCIENCE |  |
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| SECOND OPPORTUNITY / SUPPLEMENTARY EXAMINATION QUESTION PAPER |  |
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| EXAMINER(S) | Prof. JOSE QUENUM |
| MODERATOR: | Mr STANTIN SIEBRITZ |
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|  | INSTRUCTIONS |
| :--- | :--- |
| 1. Answer ALL the questions. |  |
| 2. Read all the questions carefully before answering. |  |
| 3. Number the answers clearly |  |

(Excluding this front page)

Question 1
[20 points]
The diagram in Figure 1 represents an adversarial game. Using the $\alpha-\beta$ pruning, solve the game. You will indicate the values of $\alpha$ and $\beta$ at each node and where pruning occurs.


Figure 1: Adversarial Search Problem

## Question 2 <br> [35 points]



Figure 2: a: Initial configuration; b: Goal configuration
(a) The diagram in Figure 2a represents a grid. It contains four tiles, including an empty one. Each tile is located with row and column numbers and may contain a value. For example, the tile in row 2 and column 1 contains the value 1 . In this problem, we wish to rearrange the tiles in the grid using a planning approach. The planner can execute four possible actions:

- left: moving the empty tile to the left;
- right: moving the empty tile to the right;
- up: moving the empty tile up;
- down: moving the empty tile down.

Note that these actions can only be executed when possible. Note also that when moving the empty tile to a new location, it swaps its location with the one it is replacing. We provide the following predicates to represent the knowledge base:

- above $(x, y)$ : tile $x$ is located immediately above tile $y$;
- is - left $(x, y)$ : tile $x$ is located at the left of tile $y$
- is - empty $(x)$ : tile $x$ is empty;
- $\operatorname{value}(x, y)$ : tile $x$ has value $y$;
- $\operatorname{coord}(x, y, z)$ : tile x is located at row $y$ and column $z$.

Following the STRIPS notation, define the actions as operators for the planner.
(b) Express the goal (in Figure 2b) as a well-formed formula.
difference and column difference) as a heuristic and the number of steps as path cost, generate the plan using the $A^{*}$ search strategy. You will explicitly indicate the evaluation step-by-step during the plan generation.

Question 3 . [20 points]
The Millionaire is your favourite TV show. It is a ten-round game. Except for the first round, the player can choose to play or quit at each round. When the player quits, the game ends, and $s / h e$ can collect the rewards that $s / h e$ has earned so far. When the player plays, $s / h e$ can succeed and move to the next round or fail, leading to the end of the game. Note that s/he loses all the rewards s/he has accumulated so far in the event of a failure. Note also that when the player reaches the last round, whether $s / h e$ plays or not the game ends with the appropriate reward.
Model this problem as a Markov Decision process and find the optimal policy using the value iteration approach. You will indicate the utility values during each iteration. You will use a discount factor of 0.95.

Table 1: Millionaire - Rewards and success probability

| Round | Success Probability | Reward |
| :--- | :---: | ---: |
| 1 | 0.99 | 10 |
| 2 | 0.9 | 50 |
| 3 | 0.8 | 100 |
| 4 | 0.7 | 500 |
| 5 | 0.6 | 1000 |
| 6 | 0.5 | 5000 |
| 7 | 0.4 | 10000 |
| 8 | 0.3 | 50000 |
| 9 | 0.2 | 100000 |
| 10 | 0.1 | 500000 |

## Question 4

[18 points]
(a) Company Z operates near a river which it pollutes. This has harms the fishermen who fish from the river. Company Z's profit is P. Normally, the fishermen get a profit of A. However, with the negative effect on the river, they now lose $A_{0}\left(A>A_{0}\right)$ from their profit. The fishermen and Company Z engage in litigation. Both teams will simultaneously indicate an amount. For Company Z , the amount represents their claim about the company's profit, while for the fishermen, the amount represents their profit loss. If the company's profit is less than the fishermen's lost profit, Company Z will shut down. Otherwise, it will pay a settlement to the fishermen corresponding to their lost profit
claim. Represent the strategic form of the game, describing the strategies and the payoff functions. Is it a dominant strategy for the fishermen to choose their actual loss? Why?
(b) Consider the game represented in Table 2. Determine the values of $\alpha_{1}$ and $\beta_{1}$ such that the mixed strategy with Player 1 playing the strategy $a_{0}$ with a probability of $\frac{1}{2}$ and Player 2 playing the strategy $b_{0}$ with a probability of $\frac{3}{7}$ is a Nash equilibrium.

Table 2: Game Board
Player 2

|  |  | $b_{0}$ | $b_{1}$ |
| :---: | :---: | :---: | :---: |
|  | $a_{0}$ | 2,2 | $\alpha_{1}, \beta_{1}$ |
| Player 1 | $a_{1}$ | 6,2 | 0,4 |

